

## Design of Laterally Loaded Single Piles by Using P-Y Curves and the Cone Penetration Test (CPT) in Sandy Soils

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### ABSTRACT

The aim of this paper is to present a simple method of construction of the load-transfer P-Y curves for the design of laterally loaded piles in sand based on the cone penetration test (CPT). The proposed method was developed on the basis of interpretation of 5 field tests on single instrumented piles conducted in sandy sites in France and shows a simple relationship linking the P-Y curve parameters, the cone penetration resistance and the lateral pile/soil stiffness ratio.

The validation process was carried out by direct comparison of the predicted load-deflection curves based on the proposed method to those obtained from a worldwide case history of field lateral loading tests on piles and showed a very good quality of the prediction using the proposed method.

**KEYWORDS:** Piles, Lateral load, Sand, Full-scale loading, P-Y curves, CPT test.

### INTRODUCTION

The accumulation of case histories of field lateral loading tests on piles carried out worldwide shows that the load-deflection behaviour is governed by a multitude of parameters involved in such an interaction. The theoretical modeling of laterally loaded piles is a difficult task due to the 3D response of the pile/soil system. In engineering practice, pile/soil interaction analysis is usually undertaken within the framework of a serviceability limit state (SLS) design, the pile deflection being either measured from a full-scale loading test or computed based on a variety of methods, such as elasticity-based methods (Banerjee & Davis, 1978; Budhu & Davies, 1987; Randolph, 1981; Poulos & Hull, 1992), numerical methods (Haouari & Bouafia, 2019; Khedija et al, 2020) and the P-Y curve methods (Matlock & Reese, 1960; Ménard et al., 1969; Baguelin et al, 1978; Reese & van Impe, 2001; Briaud, 2013).

In some particular pile/soil configurations (offshore

structures, monopiles of wind turbines, ... etc.) working under severe lateral loading conditions, an ultimate limit state (ULS) design should be carried out involving the lateral soil resistance (Ménard, 1969; Reese et al., 1974; Reese & van Impe, 2001).

It is nowadays recognized in engineering practice that the methods based on P-Y curves' concept offer a powerful framework to the analysis of the pile response under lateral load, with the advantage to account for the non-homogeneous distribution of the soil properties and the non-linear response of the pile/soil system. According to the P-Y curves' theory, a series of non-linear springs along the pile is used to model the pile/soil interface, where a spring subjected to the soil reaction  $P$ , at a given depth, exhibits a lateral displacement  $Y$ . A typical P-Y curve is depicted in Figure 1, where the main parameters are the initial reaction modulus  $E_{s0}$  and the lateral soil resistance  $P_u$ . According to the experience of full-scale lateral loading tests of piles, the shape of such a curve is usually non-linear and characterized by an initial linear portion corresponding to small pile deflections, as well as by a non-linear portion followed by a horizontal segment BC describing the soil failure around the pile.

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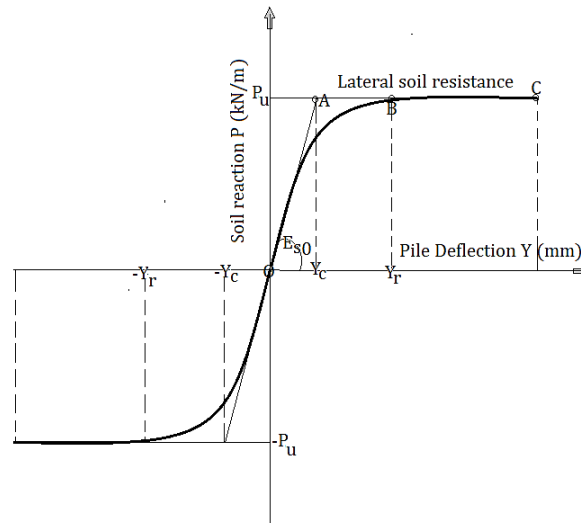


Figure (1): Schematic P-Y curve

In practice, P-Y curves are usually derived from the profiles of bending moment obtained from measurements by strain gauges along the test pile. However, successful derivation of P-Y curves from the process of double differentiation and double integration of the profile of bending moment to obtain respectively P and Y is rarely reported in the literature. Such a fact may be explained by the difficulty to derive the P-Y curves due to the high sensitivity of the lateral soil reaction P to the quality of measurements as well as to the technique of fitting and differentiation of the bending moments (Bouafia and Garnier, 1991).

Although the CPT test is one of the most commonly used *in-situ* Geotechnical tests and widely used as a foundation design tool, it is rarely recommended how to use it as an analysis tool of the pile load-deflection behavior. This paper aims at presenting a simple method to construct the P-Y curves for a single pile embedded in sandy soil based on the cone penetration test (CPT) data. This method was developed from the detailed analysis of full-scale lateral loading tests carried out on 5 fully instrumented piles in 2 sandy sites in France, within the framework of a research work undertaken by the LCPC (Laboratoire Central des Ponts & Chaussées) during the last five decades (Bouafia, 2017). An assessment of the quality of prediction of the proposed method was carried out by a direct comparison of the predicted load-deflection response of a small-sized database of full-scale single piles loaded in sandy soils to the experimental results.

### Brief Review of the Methods of P-Y Curves

Reese and Matlock (1956) were the pioneer researchers who studied the P-Y curves by introducing the concept of lateral reaction modulus, initially defined by Winkler (1867). The proposed P-Y curves were bilinearly shaped, assuming an elastic plastic response at the pile soil/interface depicted by the portion OABC in Figure 1 (Reese and Matlock, 1956).

As from the sixties, the *in-situ* tests, such as the pressure meter (PMT) and the CPT tests, have become widely used tools of analysis and design of pile foundations. The PMT test was used by Louis Ménard, the inventor of this test and the pioneer of the pressure meter theory and subsequent studies proposed many refinements and improvements of the basic method (Dunand, 1981; Baguelin et al., 1978; Robertson et al., 1984; Briaud et al, 1985; Bouafia, 2007).

The CPT test has many advantages compared to the PMT test, the main of which are the continuity of measurement of the soil resistance and the simplicity of the experimental procedure. However, the PMT test has the advantage to obtain a complete stress-strain curve at a given depth, which allows a direct evaluation of the soil stiffness. Nonetheless, in light of modern theories, like the theory of cavity expansion (Ladanyi, 1963; Vesic, 1972; Ladanyi and Longtin, 2005) and the theory of strains' path (Baligh, 1985; Baligh and Levadoux, 1986), the cone resistance clearly depends on the soil compressibility and may thus be seen as a tool of indirect evaluation of the soil stiffness. Moreover, some experimental research works demonstrated the possibility of correlation of the stiffness

of sandy soils to the cone resistance  $q_c$  (Jamiolkovski, 1988; Lunne et al., 1997).

The first approach of construction of a P-Y curve based on the cone penetration resistance  $q_c$  was proposed by Schmertmann (1978) who recommended an elastic perfectly plastic function for the P-Y curve (curve OABC in Figure 1), where the lateral reaction modulus  $E_{s0}$  depends on  $q_c$  and the pile diameter  $B$ , whereas the lateral soil resistance  $P_u$  is taken equal to 11% of  $q_c B$  in loose sand and 22% of  $q_c B$  in dense sand.

A series of centrifuge tests on a 0.36-m diameter steel pile driven into calcareous sand led Novello (1999) to propose a description of the P-Y curve by a power function as follows:

$$P = \min \left\{ 2B(\gamma'z)^{1/3} q_c^{2/3} \left( \frac{Y}{B} \right)^{1/2}, B \cdot q_c \right\} \quad (1)$$

where  $P$ ,  $Y$ ,  $z$ ,  $B$  and  $\gamma'$  are respectively the lateral soil reaction, the pile deflection, the soil depth, the pile diameter and the submerged unit weight, expressed respectively in kN/m, m, m, m and kN/m<sup>3</sup>. The lateral soil resistance was simply defined by the product  $q_c B$ .

The above equation was modified by Dyson and Randolph (2001) to better fit their experimental results of centrifuge tests on laterally loaded piles driven into a calcareous sandy soil, as follows:

$$P = 2.84\gamma' B^2 \left( \frac{q_c}{\gamma' B} \right)^{0.72} \left( \frac{Y}{B} \right)^{0.64} \quad (2)$$

Based on an extensive centrifuge test on piles embedded in dry dense to very dense sand, Bouafia (2009) proposed hyperbolic shaped P-Y curves and showed the possibility to correlate the lateral reaction modulus  $E_{s0}$  to the drained initial constraint modulus  $M_0$  and  $P_u$  to  $q_c$ , where the modulus  $M_0$  was empirically correlated to  $q_c$  as proposed by Eslaamizaad and Robertson (1996) who worked on unaged and uncemented silica sands in a calibration chamber.

Suryasentana and Lehane (2014a) performed a parametric numerical study based on a 3D finite element model of a single pile embedded in sand and proposed the following equation:

$$P = 2.4\gamma z B \left( \frac{q_c}{\gamma z} \right)^{\frac{2}{3}} \left( \frac{z}{B} \right)^{\frac{3}{4}} \left( 1 - \exp \left\{ -6.2 \left( \frac{z}{B} \right)^{-1.2} \left( \frac{Y}{B} \right)^{0.89} \right\} \right). \quad (3)$$

For short rigid piles, Kim et al. (2015) proposed an

equation of the lateral resistance  $P_u$  based on the work of Lee (2010) as follows:

$$P_u = 2.775 B q_c^{0.391} \sigma_m'^{0.609} \quad (4)$$

where  $\sigma'_m$  is the mean effective stress. Note that in all these equations, the soil reaction  $P$  varies as a power of  $q_c$  whereas a simpler approach consists of considering a direct proportionality between  $P$  and  $q_c$  as will be shown hereafter in light of experimental results obtained from field lateral tests on piles.

The French standard NF P94-262 for deep foundations, accompanying the Eurocode 7, recommends for piles in sand under permanent lateral loading an elastic perfectly plastic P-Y curve defined by a lateral reaction modulus  $E_{s0}$  equal to  $(2.25q_c)$  and a soil resistance  $P_u$  represented by an asymptote equal to  $(q_c B/13)$ . Under short-duration loads,  $E_{s0}$  is doubled and  $P_u$  is kept the same as under permanent loads (AFNOR, 2012).

It should be noted that the previous formulations ignore the effect of the pile/soil stiffness ratio on the load-deflection behaviour of a laterally loaded pile, which implicitly leads to the application of these methods for both short rigid piles and long flexible piles, in contrast with the experimental observations of many full-scale pile tests (Bouafia, 2007). In fact, it is possible to correlate the reaction modulus  $E_{s0}$  and the soil resistance  $P_u$  at a given depth  $z$  to  $q_c$  and the pile properties on the basis of the following equation:

$$f(q_c^*, E_p I_p, D, B, P_u, E_{s0}) = 0 \quad (5)$$

where  $q_c^*$  is the net cone resistance taking into account the initial stress state and given by:

$$\text{where } q_c^*(z) = q_c(z) - \sigma_{v0}(z) \quad (6)$$

where  $q_c$  and  $\sigma_{v0}(z)$  are, respectively, the cone resistance and the initial vertical overburden pressure at depth  $z$ .

The pile flexural stiffness, the pile embedded length and the pile diameter (or the dimension perpendicular to the lateral load direction) are respectively denoted by  $E_p I_p$ ,  $D$  and  $B$ . Equation (5) may be transformed by a dimensional analysis based on the Buckingham's theorem which leads to:

$$g\left(\frac{E_{s0}}{q_c^*}, \frac{P_u}{q_c^* B}, \frac{D}{B}, \frac{E_p I_p}{q_c^* D^4}\right) = 0. \quad (7)$$

This equation relates 4 dimensionless variables, whereas Equation (6) relates 6 physical parameters. The first term is called "the modulus number" and hereafter noted  $K_E$  as follows:

$$E_{s0} = K_E q_c^*. \quad (8)$$

Similarly, the second term is called "the lateral resistance factor" and noted  $K_c$  leading to compute the soil resistance as follows:

$$P_u = K_c q_c^* B. \quad (9)$$

The third term is the pile slenderness ratio and the last one is called "the lateral pile/soil stiffness ratio" and noted  $K_R$ . On the basis of equation 7,  $K_E$  as well as  $K_c$  depend on  $K_R$  and  $D/B$ . Moreover, since  $K_E$  corresponds to small pile displacements and  $K_c$  corresponds rather to large displacements, they should be independent. Equation (7) may therefore be uncoupled to the two following equations:

$$K_E = \frac{E_{s0}}{q_c} = h\left(q_c^*, K_R, \frac{D}{B}\right); \quad (10)$$

$$K_c = \frac{P_u}{q_c B} = j\left(q_c^*, K_R, \frac{D}{B}\right). \quad (11)$$

Determination of the functions  $h$  and  $j$  leads to practical formulation of the P-Y curves' parameters, as given by Equations (8) and (9). The experimental analysis of the coefficients  $K_E$  and  $K_c$  on the basis of the lateral loading test on full-scale single piles offers a pragmatic framework.

### Description of Field Tests on Piles

#### Geotechnical Aspect of the Experimental Sites

Within the scope of a research project undertaken during 1987-88, 5 full-scale lateral loads were applied in 2 sandy sites in France. The first site, noted  $S_1$ , is located in Châtenay-sur-Seine, 70 km south-east of Paris and the second one, noted  $S_2$ , is located in Le-Rheu, 5 km south-west of Rennes. Site  $S_1$  is composed of two layers of a poorly graded sand ( $S_p$ ) called Fontainebleau sand; the

first layer has a thickness of 1.80 m of dense sand ( $I_D=57\%$ ) overlying a loose layer (density index  $I_D=37\%$ ) with a thickness of 1.40 m. Site  $S_2$  is composed of poorly graded clean sand ( $S_p$ ) and the groundwater level is 10 m deep. The average water content of the sand above water table is 8%, which corresponds to a saturation degree of 31%. Geotechnical *in-situ* tests, notably the PMT, CPT and DPT (dynamic penetration test), were carried out at the location of test piles and analyzed elsewhere (Bouafia, 2007). The CPT test was carried out in both sites with a conic tip having an apex angle of  $60^\circ$ , a diameter of 35.7 mm and a sleeve friction having an area of  $150 \text{ cm}^2$ , which is in accordance with the international standard ISO-22476-1 (AFNOR, 2013).

The profile of the cone resistance  $q_c(z)$ ,  $z$  being the depth of measurement, is usually irregular due to the presence of many peaks registered, which is mainly due to the performance of the penetration device rather than to a relatively high local penetration resistance. In practice, the profile  $q_c(z)$  is interpreted according to different approaches, like smoothing, interpolation or filtration. During the development of the proposed CPT-based method, the conventional procedure of interpretation of the profile  $q_c(z)$  was adopted, consisting in filtering the profile  $q_c(z)$  by suppressing and interpolating the peaks of resistance, which implies the use of a relatively smooth profile of cone resistance. The method presented hereafter is then based on a filtered profile and not on the gross profile of resistance.

### Piles

The test piles are open-ended steel pipes and are equipped by pairs of strain gauges along two diametrically opposite axes. Piles  $T_5$ ,  $T_{10}$  and  $T_{15}$  were jacked in site  $S_1$  and piles  $P_1$  and  $P_2$  were bored in site  $S_2$ . The margin of the ratio embedded length /diameter of the test piles lies between 5.5 and 15.3.

As shown in Figure 2, a hydraulic jack in contact with a concrete block of reaction was used to apply the lateral load which is measured by a high-precision electric load cell.

The program of loading consisted of a series of monotonic lateral loads at the pile top; the duration of each load increment was 15 minutes in site  $S_1$  and 2 hours in site  $S_2$ .

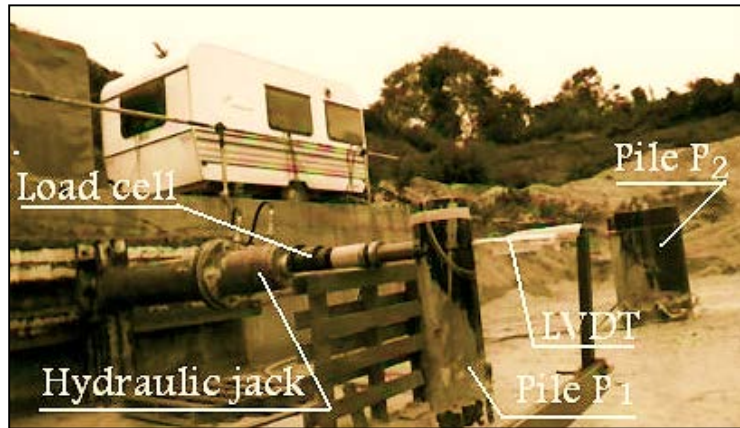
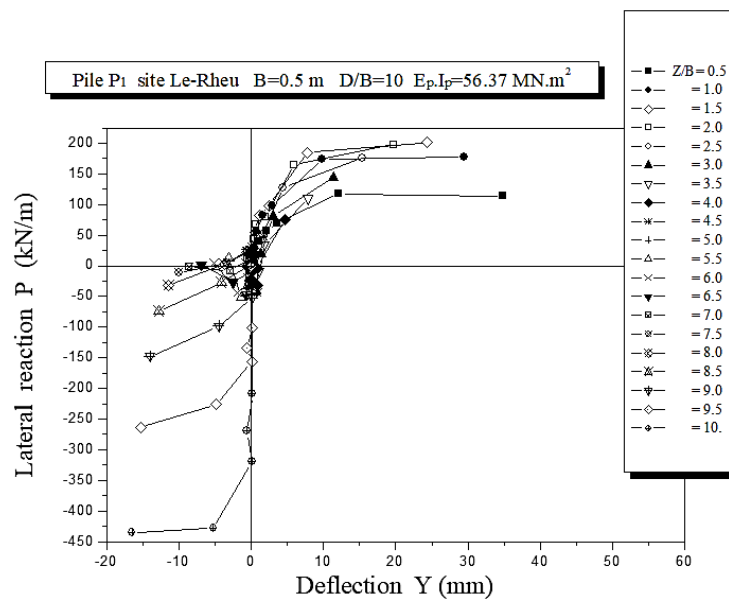


Figure (2): Experimental configuration of the test piles P<sub>1</sub> and P<sub>2</sub> in site S<sub>2</sub>

### Construction of Experimental P-Y Curves

For a given load increment, the profile of the measured bending moment  $M(z)$  was obtained from the axial strains provided by the strain gauges along the pile. The fitting process of the bending-moment profile was carried out by using quintic spline functions or polynomial functions, the choice of the fitting function being governed by the criterion of equilibrium of the pile under the lateral reaction profile  $P(z)$  and the load applied at the pile top within a given tolerance (Bouafia & Garnier, 1991). The lateral displacement  $Y(z)$  along the pile may easily be obtained by two successive integrations of  $M(z)$ . Moreover, the soil reaction  $P(z)$  is determined by two successive differentiations of  $M(z)$

and then the P-Y curve at any depth may be constructed. In Figure 3, a typical set of experimental P-Y curves for the pile P<sub>1</sub> is illustrated, where it can be noticed that there is an inherent non-linearity in the shape of the curves as well as a regular increase in soil stiffness with depth. These curves are marked by a simultaneous change in sign for the deflection  $Y(z)$  and the soil reaction  $P(z)$  at about 6 diameters of depth, which is in accordance with the Winkler's hypothesis, according to which  $P(z)$  and  $Y(z)$  have the same sign. Moreover, for relatively large deflections, exceeding a threshold of about 3% of  $B$ , the P-Y curves exhibit asymptotic values, indicating a full mobilization of the lateral soil resistance.



### Analysis of P-Y Curve Parameters

To derive the P-Y curve parameters; namely,  $E_{s0}$  and  $P_u$ , the experimental P-Y curves were fitted on the basis

of a simple analytical function called **PARECT** (**PAR**abola-**RECT**angle), which is able to capture the non-linear shape of the curve (portion OB in Figure 1), as well as the mobilization of the soil resistance described by an asymptote (portion BC in Figure 1) as from a threshold deflection  $Y_R(z)$  called "reference deflection". The **PARECT** function is defined as follows:

$$P(z) = E_{s0}(z) \cdot Y(z) \cdot \left(1 - \frac{Y(z)}{2Y_R(z)}\right). \quad (12)$$

Since at the deflection  $Y_R$  the soil reaction  $P$  reaches  $P_u$ , the P-Y curve may be written as:

$$P(z) = 2P_u(z) \frac{Y(z)}{Y_R(z)} \left(1 - \frac{Y(z)}{2Y_R(z)}\right). \quad (13)$$

From the two previous equations, the reference deflection should be equal to:

$$Y_R(z) = 2 \frac{P_u(z)}{E_{s0}(z)}. \quad (14)$$

Compared to some functions used in practice to describe the P-Y curve (hyperbolic, exponential, hyperbolic tangent, ... etc) giving an infinite value to  $Y_R$ , the **PARECT** function provides rather a finite value and consequently offers a more realistic description of the pile load-deflection behaviour.

Experimental P-Y curves were fitted by the **PARECT** function on the basis of the least-squares technique, which led to construct the profiles of  $E_{s0}$  and  $P_u(z)$  of each pile tested. Further correlations of these profiles with that of the net cone resistance  $q_{ce}^*(z)$  will lead, as will be seen hereafter, to determine the functions  $h$  and  $J$  defined respectively in Equations (10) and (11).

### The Lateral Pile/Soil Stiffness Ratio

In most cases, the profile  $q_{ce}^*(z)$  is marked by a non-negligible variation with depth. To account for such a non-homogeneity, an equivalent net cone resistance  $q_{ce}^*$  is defined as follows:

$$q_{ce}^* = \frac{1}{D_e} \int_0^{D_e} q_c^* \cdot dz \quad (15)$$

where  $D_e$ , called "the effective embedded length" of the pile, is the depth below which the pile segments do not respond to the lateral loading at the pile top and defined as:

$$D_e = \min\{D, \pi L_0\} \quad (16)$$

where the elastic length (or transfer length)  $L_0$  is defined by:

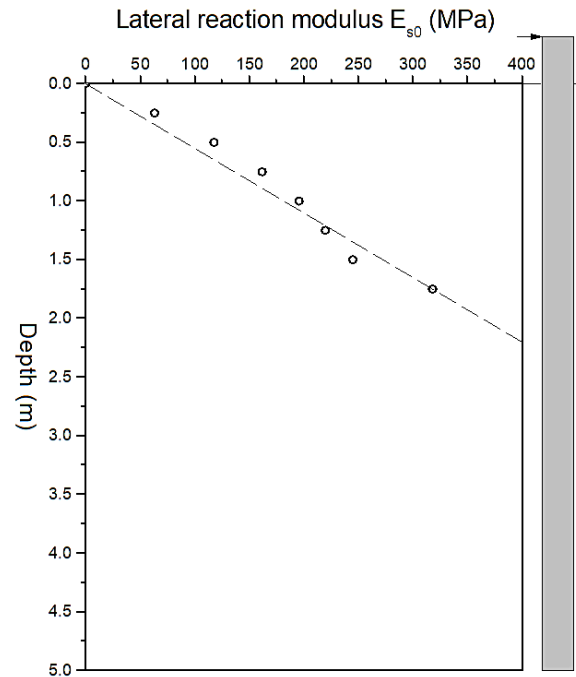
$$L_0 = \sqrt[4]{\frac{E_p \cdot I_p}{K_E \cdot q_{ce}^*}}. \quad (17)$$

The lateral pile/stiffness ratio already defined in Equation (7) is written as follows:

$$K_R = \frac{E_p \cdot I_p}{q_{ce}^* \cdot D^4}. \quad (18)$$

### The Lateral Reaction Modulus $E_{s0}$

It was found for all the test piles that the profile of the reaction modulus  $E_{s0}(z)$  is linear, corresponding to a usual distribution of the soil stiffness in homogeneous granular soils belonging to the category of Gibson's soils. In Figure 4, a typical profile of  $E_{s0}(z)$  for the pile  $P_2$  is illustrated.



**Figure (4): Typical profile of the lateral reaction modulus for pile  $P_2$**

Having a slenderness ratio  $D/B$  equal to 5.5, the pile  $P_2$  should be considered rather as a pier exhibiting a different behaviour than that of a pile. The analysis of

the experimental values of the modulus number  $K_E$  showed a singular value of  $K_E$  of  $P_2$  with respect to other piles, which leads to limit the analysis of  $K_E$  to piles characterized by  $D/B$  greater than or equal to 10. Moreover, according to the values of  $K_R$  for the piles tested, they are classified as semi-rigid piles ( $K_R \geq 2.9 \times 10^{-2}$ ). Due to limited data regarding the flexible piles, it was suggested to extend the value of  $K_E=5.1$  corresponding to  $K_R=2.9 \times 10^{-2}$  for all the flexible piles, provided that this extension will be subsequently validated by analyzing the response of a representative case history of experimental flexible piles.

The study of the function  $h$  formulated by Equation (10) showed that the modulus number  $K_E$  depends slightly on the slenderness ratio  $D/B$  and varies as a power function of the lateral pile/soil stiffness ratio  $K_R$

as follows:

$$K_E = \begin{cases} \frac{1}{10} K_R^{-1.1} & \text{if } K_R > 0.029; \\ 5.1 & \text{if } K_R < 0.029. \end{cases} \quad (19)$$

According to this equation, the modulus number decreases with the pile/soil stiffness ratio, which means that a flexible pile behaves with a greater value of  $K_E$  than that of a rigid pile. Moreover, based on Equation (18),  $K_E$  decreases with the flexural stiffness  $E_p I_p$  and increases with the pile length  $D$ .

The equation of  $K_E$  is only valid for long piles having  $D/B$  greater than or equal to 10. Figure 5 illustrates in a bi-logarithmic scale the variation of the modulus number as a function of  $K_R$ .

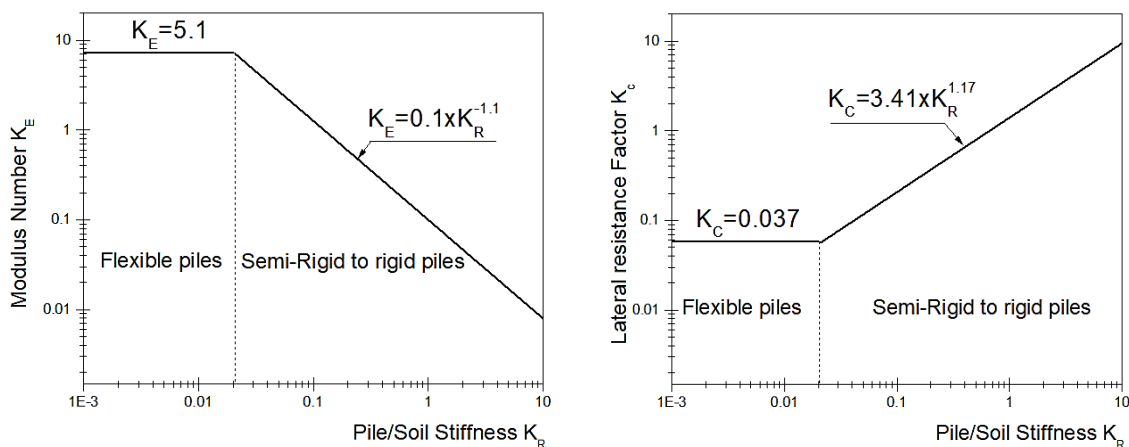


Figure (5): Diagrams of the P-Y curve parameters  $K_E$  and  $K_c$

Since the test piles were jacked or bored, it seems that the installation procedure has a relatively little effect on the reaction modulus for semi-rigid piles, which is in accordance with the findings of Bouafia and Garnier (1991) from centrifuge tests.

**The Lateral Soil Resistance  $P_u$**

Similarly, the function  $j$  defined by Equation (11) was found depending on the lateral pile/soil stiffness and was formulated by fitting its experimental values by a power function as follows:

$$K_c = \begin{cases} 3.41 \times K_R^{1.17} & \text{if } K_R > 0.029; \\ 0.037 & \text{if } K_R < 0.029. \end{cases} \quad (20)$$

It is interesting to highlight that this equation shows an increase of  $K_c$  with the pile/soil stiffness ratio  $K_R$ . Consequently, the soil around a rigid pile is characterized by a greater value of  $K_c$  than that of a flexible pile and mobilizes a greater soil resistance. Furthermore, according to Equation (18),  $K_c$  increases with  $E_p I_p$  and decreases with length  $D$ .

This formula, illustrated by Figure 5, is also limited to long piles having  $D/B$  greater than or equal to 10 and provides a substantial improvement of previous studies (Bouafia, 2009; 2010; 2014; 2017).

The values of  $K_c$  proposed by Schmertmann (1978) are 0.11 and 0.22, respectively in loose and dense sand independently of the pile stiffness, whereas Novello (1999) suggested a value of 1.0 which is much greater

than that of Schmertmann. Moreover, on the basis of Equation (4) proposed by Kim et al. (2015), the coefficient  $K_c$  may be derived with a somewhat laborious formulation depending on  $q_c$  as well as on the depth. Finally, the French standard prescribes a value of 0.077 for  $K_c$ . Compared to these values, those given by Equation (19) are smaller, particularly for flexible piles, but they offer the advantage to take into consideration the pile/soil stiffness and provide relatively conservative values of  $K_c$ .

Regarding the modulus number  $K_E$ , previous studies (Novello, 1999; Disan and Randolph, 2001; Suryasentana and Lehane, 2014) proposed power functions expressed by Equations (1) to (3) serving to construct the P-Y curve point-by-point, but not allowing to derive the lateral reaction modulus. The French standard prescribed a value of 2.25 for  $K_E$  regardless of the value of the lateral pile/soil stiffness  $K_R$ , which means that it is applicable to flexible as well as to rigid piles.

### The Reference Deflection $Y_R$

On the basis of Equations (14), (8) and (9), the reference deflection may be written as follows:

$$Y_R(z) = 2 \frac{P_u(z)}{E_{s0}(z)} = 2 \frac{K_c B}{K_E} \quad (21)$$

According to Equations (19) and (20),  $Y_R$  for flexible piles ( $K_R < 2.9 \times 10^{-2}$ ) does not depend on  $K_R$  and takes a constant value of 1.5%. For semi-rigid to rigid piles, fitting the experimental values of  $K_c$  and  $K_E$  leads to the following power function with a value of the correlation coefficient  $R$  equal to 99.5%:

$$\frac{Y_R}{B} = 109 [K_R]^{2.5} \quad (22)$$

For comparison, the French standard P94-262 specifies that  $Y_R/B$  is equal to 3.4%, whereas in the method of Reese et al. (1974),  $Y_R/B$  is equal to 3.75%. Finally, a widely used design criterion is the conventional value of 10% of  $B$ . As can be seen from Equation (22) and Figure 6, the reference deflection increases as a power of the lateral pile/soil stiffness in contrast with the traditional methods of P-Y curves ignoring this parameter, thereby providing a reference deflection applicable to flexible as well as to rigid piles.

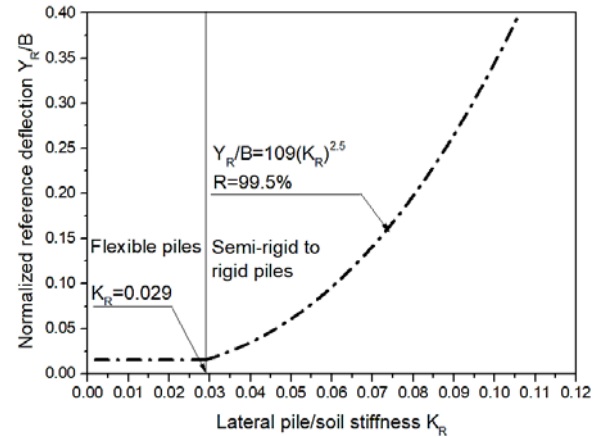


Figure (6): Chart of the normalized reference deflection  $Y_R/B$

### Step-by-Step Procedure of Construction of P-Y Curves

The following methodology allows a practical analysis of a laterally loaded pile in sand on the basis of P-Y curves constructed from the CPT data:

1. Filter the profile of cone resistance by eliminating the peaks of resistance and simply replacing them by a linear interpolation.
2. Sub-divide the soil along the pile into  $N$  thin horizontal segments in such a way that  $q_{c^*}$  exhibits a linear variation within any segment. The value of  $q_{c^*}$  at the mid-segment is therefore representative of all the segment.
3. Assume that the pile is semi-rigid or rigid. From Equation (16), one obtains:  $D_e = D$ .
4. Compute  $q_{ce^*}$  according to Equation (15) by replacing the integration formula by the summation of trapezes.
5. Compute  $K_R$  according to Equation (18).
6. Compute  $K_E$  by Equation (19) or determine it from Figure 5.
7. Compute  $L_0$  by Equation (17).
8. Compute  $D_e$  of the pile from Equation (16). If  $D_e < D$  (case of flexible pile), then an iterative process is carried out by repeating steps from 4 to 8 until convergence of  $K_R$ .
9. Compute the values of  $E_{s0}$  and  $P_u$  for each segment from Equations (8) and (9), respectively.
10. Use Equation (12) or Equation (13) to construct the P-Y curve for each segment along the pile.
11. Use a software based on the theory of P-Y curves to analyze the pile response, like the software SPULL



(single pile under lateral loads) developed at the University of Blida since 1999 (Bouafia, 2007). This software is a freeware available upon request.

### Validation of the Proposed Method

#### Description of the Case Histories

The predictive capability of the proposed CPT-based

P-Y curves' method was assessed by predicting the load-deflection behaviour of test piles subjected to monotonic loading in sandy deposits. Summarized in Table 1 are the main Geo-technical and physical properties of the pile/soil systems. For easy access to the data, the piles analyzed are identified as mentioned in their original references.

**Table 1. Features of the pile/soil systems used in full-scale tests**

Site	Pile	D (m)	D/B	$E_p I_p$ (MN.m <sup>2</sup> )	$q_{ce}^*$ (MPa)	$D_e$ (m)	$K_R$	Reference
S <sub>3</sub>	3-12	20.4	57.3	61	10.24	3.94	$3.44 \times 10^{-5}$	Bouafia (2007)
	3-13	20.4	57.3	61	10.24	3.94	$3.44 \times 10^{-5}$	Bouafia (2007)
S <sub>4</sub>	DS-4	2.73	10.0	10.35	21.77	2.10	$8.56 \times 10^{-3}$	Ross et al. (2019)
S <sub>5</sub>	PS-3	4.35	12.8	40.0	12.30	3.40	$9.10 \times 10^{-3}$	Li et al. (2014)
S <sub>6</sub>	PS-5	5.00	14.7	40.0	13.90	3.28	$4.60 \times 10^{-3}$	Li et al. (2014)
	PS-6	7.00	20.6	40.0	13.90	3.28	$1.20 \times 10^{-3}$	Li et al. (2014)
S <sub>7</sub>	UWA-1	3.50	15.56	2.42	3.43	2.30	$4.70 \times 10^{-3}$	Suryasentana & Lehane (2014b)
S <sub>8</sub>	UWA-2	6.00	17.65	11.50	13.30	2.40	$6.70 \times 10^{-4}$	Suryasentana & Lehane (2014b)
S <sub>9</sub>	PD	11.5	35.5	30.0	3.96	4.68	$4.30 \times 10^{-4}$	Rollins et al. (2005)
S <sub>10</sub>	PF	13.8	23.0	291.8	2.81	9.00	$2.82 \times 10^{-3}$	Rollins et al. (2005)
S <sub>11</sub>	#2	15.0	31.2	70.0	6.42	5.10	$2.10 \times 10^{-4}$	Reese & van impe (2001)

Site S<sub>3</sub> is located at the Lock & Dam 26 near the Mississippi river and composed of 20-m thick poorly graded medium-to-coarse sand with gravel overlying a bedrock of hard limestone. Two identical HP-14x73 piles socketed in the limestone bedrock were subjected to lateral loading increments, where each pile served during tests as a reaction beam to the other one.

Site S<sub>4</sub> is located at Dunkirk, about 300 km north of Paris, being composed of fine-to-medium sand and the test pile is a steel pipe installed by vibratory driving into the site.

Sites S<sub>5</sub> and S<sub>6</sub> are both located at Blessington, about 35 km south-west of Dublin, Ireland and composed of heavily over-consolidated very dense sand with a density index nearly equal to 100%. The test piles are three identical open-ended steel pipe piles driven into embedded lengths varying from 4.3 to 7 m.

Site S<sub>7</sub> is located at Shenton Park, Perth, Western Australia and composed of a deposit of a dry loose-to-medium dense sand and the test pile is a grouted pile.

Site S<sub>8</sub> is located at north Perth, Western Australia

and composed of dense sandy soil deposit, while the test pile is a CFA bored pile.

Site S<sub>9</sub> is located at Treasure Island, San-francisco Bay, California and composed of poorly graded silty sand along the pile with the presence of a silty clay layer with a thickness of 1.60 m and outside the effective length  $D_e$  of the pile. The test pile is a driven steel pipe pile loaded under a controlled displacement rate of 9 mm/s.

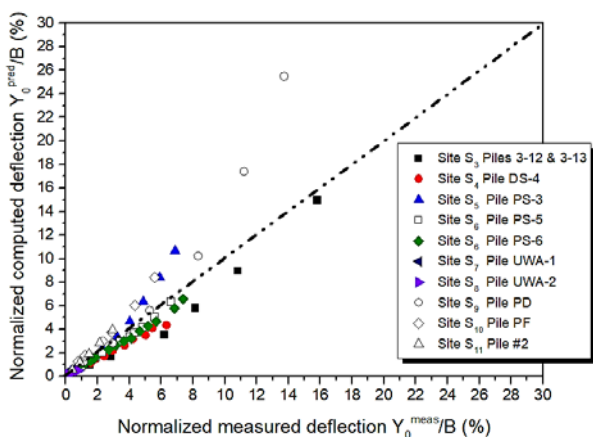
Site S<sub>10</sub> is located at Treasure Island, but composed of a saturated poorly graded loose sand with the presence of a low-plasticity clayey layer with a thickness of 1.2 m above the pile base. This layer does not affect the pile response, since it is outside the effective length  $D_e$ . The test pile is a cast-in-steel-shell bored pile.

The last site, noted S<sub>11</sub>, is located at Arkansas River, Mississippi and composed of poorly-graded sand with small traces of fines and the test pile is a steel pipe pile.

### Discussion of the Results of Validation

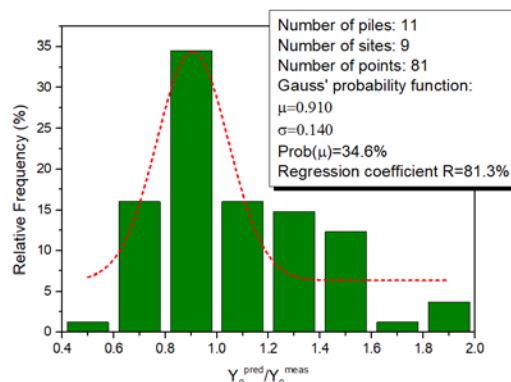
P-Y curves of each pile analysed were generated

from the CPT data of the experimental site according to the methodology mentioned above and input into the software SPULL to simulate the load-deflection curve of each pile. Figure 7 illustrates a direct comparison of the predicted pile deflections  $Y_0$  at ground level to the ones measured up to 16% of the pile diameter. It can be noticed that there is a very good accordance between predicted and measured deflections, particularly for normalized pile deflections less than 8%. The ratio of predicted to measured deflection  $Y_0^{pred}/Y_0^{meas}$  is characterized by an average value of 1.07 and a coefficient of variation of 30%. Moreover, Figure 8 illustrates the histogram of the 81 points of comparison through the random variable  $Y_0^{pred}/Y_0^{meas}$ . Fitting this histogram by the Gauss' density function leads to a mean value  $\mu$  of 0.91, a standard deviation  $\sigma$  of 0.14 and a confidence interval [0.81, 1.14] for the mean value at a level of 95% of confidence, which is very encouraging seeing the multitude of approximations made during the process of development of this method.



**Figure (7): Comparison of predicted and measured pile deflections**

In light of this process of validation, it can be seen that the proposed method of construction of P-Y curves on the basis of the CPT tests has a good predictive capability capturing many aspects of the pile/soil interaction; namely, the variability of the soil properties, the effect of different techniques of the pile installation and the non-linear response of the pile.



**Figure (8): Histogram of the ratio  $Y_0^{pred}/Y_0^{meas}$**

### CONCLUSIONS

In this paper, an empirical method to construct the P-Y curves for single piles in sand based on the cone penetration test CPT was proposed. A detailed interpretation of 5 full-scale lateral loading tests of instrumented piles in 2 sandy soils led to derive the parameters of the experimental P-Y curves in correlation with cone resistance  $q_c$ . It was found that the lateral reaction modulus and the lateral soil resistance vary as power functions of the lateral pile/soil stiffness ratio, on the basis of which a parabola-rectangle function was proposed to describe the P-Y curves in sand and a step-by-step procedure of analysis of the load-deflection response of a single pile under lateral load in sand was proposed.

An assessment of the predictive capability of the proposed method undertaken by predicting the pile/soil response of 11 test piles in full-scale tests in 9 sites worldwide showed a very good accordance between the predicted pile deflections and the measured ones, which makes encouraging seeing the multitude of approximations made during the process of development of this method.

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### Conflict of Interest

The author declares that there is no conflict of interest regarding this work.

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